Question 24

What is the dot product of a vector with the cross product that this vector has with another vector?

Solution

The dot product that a vector $\overrightarrow{\mathbf{A}}$ has with the cross product of this vector with another vector $\overrightarrow{\mathbf{B}}$ is

$$\overrightarrow{\mathbf{A}} \cdot \left(\overrightarrow{\mathbf{A}} \times \overrightarrow{\mathbf{B}} \right) = 0.$$

The vector $\overrightarrow{\mathbf{A}} \times \overrightarrow{\mathbf{B}}$ is perpendicular to both $\overrightarrow{\mathbf{A}}$ and $\overrightarrow{\mathbf{B}}$, and the dot product of $\overrightarrow{\mathbf{A}}$ with any vector perpendicular to it is zero.